

Protein Self-Association Induced by Macromolecular Crowding: A Quantitative Analysis by Magnetic Relaxation Dispersion

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ABSTRACT In the presence of high concentrations of inert macromolecules, the self-association of proteins is strongly enhanced through an entropic, excluded-volume effect variously called macromolecular crowding or depletion attraction. Despite the predicted large magnitude of this universal effect and its far-reaching biological implications, few experimental studies of macromolecular crowding have been reported. Here, we introduce a powerful new technique, fast field-cycling magnetic relaxation dispersion, for investigating crowding effects on protein self-association equilibria. By recording the solvent proton spin relaxation rate over a wide range of magnetic field strengths, we determine the populations of coexisting monomers and decamers of bovine pancreatic trypsin inhibitor in the presence of dextran up to a macromolecular volume fraction of 27%. Already at a dextran volume fraction of 14%, we find a 30-fold increase of the decamer population and 510^5 -fold increase of the association constant. The analysis of these results, in terms of a statistical-mechanical model that incorporates polymer flexibility as well as the excluded volume of the protein, shows that the dramatic enhancement of bovine pancreatic trypsin inhibitor self-association can be quantitatively rationalized in terms of hard repulsive interactions.

INTRODUCTION

The importance of excluded-volume interactions for the solution behavior of proteins was first recognized in studies of the effect of polymers on protein partitioning (Ogston and Phelps, 1960) and solubility (Laurent, 1963; Atha and Ingham, 1981), which laid the foundations for the current widespread use of nonadsorbing polymers, like polyethylene glycol, for protein separation (Albertsson, 1986) and crystallization (McPherson, 1985). More recently, the realization that macromolecules occupy 20–30% of the intracellular volume has provided a biological motivation for studying the effects of nominally inert background macromolecules on protein association equilibria and rate processes (Minton, 1981, 1998, 2000; Ellis, 2001). Now loosely referred to as “macromolecular crowding”, such entropic, excluded-volume effects are thought to play important roles in protein folding (van den Berg et al., 1999; Qu and Bolen, 2002; Sasahara et al., 2003), protein self-association into functional native oligomers (Lindner and Ralston, 1995; Rivas et al., 1999, 2001; Zorrilla et al., 2004a) or amyloid aggregates (Hatters et al., 2002), intracellular compartmentation (Walter and Brooks, 1995; Hancock, 2004), and cell volume regulation (Garner and Burg, 1994; Al-Habori, 2001).

Addition of inert macromolecules to a protein solution shifts equilibria toward the more compact state because this minimizes the volume excluded to the inert macromolecules.

Under typical physiological conditions, macromolecular crowding is therefore a powerful driving force for protein self-association, which may increase the association constant by several orders of magnitude as compared to dilute *in vitro* conditions. Whereas theoretical predictions of macromolecular crowding effects abound, there are remarkably few experimental studies of this universal phenomenon. The principal experimental challenge is to resolve and quantify populations of protein oligomers in dynamic equilibrium. This task is further complicated by the background of abundant macromolecular crowding agent. One of the few techniques that has been applied to this problem is analytical ultracentrifugation, where tracer sedimentation equilibrium data yield an apparent buoyant molar mass, which, after certain approximations, provides the weight-average molar mass of the self-associating protein (Rivas et al., 1999). Because this technique does not resolve the different oligomers, the interpretation becomes somewhat model dependent.

In this work, we demonstrate that the macromolecular crowding effect can be studied in a direct way by an NMR technique known as magnetic relaxation dispersion (MRD). The MRD technique has recently been used to characterize quantitatively the self-association of bovine pancreatic trypsin inhibitor (BPTI) (Gottschalk et al., 2003a), bovine β -lactoglobulin (Gottschalk et al., 2003b), and hen lysozyme (Gottschalk and Halle, 2003), in all cases without crowding agent. By recording the solvent proton spin relaxation rate over a wide range of magnetic field strengths, it is possible to resolve (in the frequency domain) protein oligomers with different rotational diffusion coefficients and to determine the populations of coexisting oligomers. Here, we use the MRD technique to study the BPTI monomer-decamer equilibrium (Hamiaux et al., 2000; Gottschalk et al., 2003a) in the

Submitted November 8, 2004, and accepted for publication December 28, 2004.

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0006-3495/05/04/2855/12 \$2.00

doi: 10.1529/biophysj.104.055871

presence of dextran as a crowding agent. We find that BPTI self-association is strongly enhanced by the polymer, with a 30-fold increase of the decamer population and 510^5 -fold increase of the association constant at a dextran volume fraction of merely 14%.

Dextran is commonly used as a crowding agent because it is uncharged and does not adsorb to protein surfaces (Laurent, 1963; Lindner and Ralston, 1995; Rivas et al., 1999; van den Berg et al., 1999; Qu and Bolen, 2002; Hatters et al., 2002; Sasahara et al., 2003). On the other hand, the conformational flexibility of the dextran polymer chain complicates the statistical-mechanical analysis of the crowding effect. In contrast to previous work, we take the flexibility into account explicitly in the theoretical analysis (Lue, 1998). We find that the MRD data can be quantitatively accounted for by a hard-repulsion (excluded-volume) interaction and a Kuhn length for dextran consistent with light-scattering results. Our theoretical analysis also incorporates, in a self-consistent manner, the crowding effect of the protein itself.

MATERIALS AND METHODS

Materials and sample preparation

Bovine pancreatic trypsin inhibitor was supplied by Bayer HealthCare AG (Trasylol, lot no. 9104, 97% purity by high-performance liquid chromatography). After exhaustive dialysis to remove residual salt the protein was lyophilized. Dextran, manufactured by sucrose fermentation with *Leuconostoc mesenteroides* bacteria (strain B-512), limited hydrolysis, ethanol fractionation, and spray drying, was obtained from Sigma (product no. D9260). According to the manufacturer, the mean molecular mass was $\bar{M} = 10.4 \text{ kg mol}^{-1}$ (determined by size exclusion chromatography), which corresponds to a mean degree of polymerization of $\bar{\mu} = 64.1$. The residual water content of the dextran preparation was taken to be 5%.

Samples for MRD measurements were prepared by dissolving, at room temperature, dextran and/or BPTI in millipore water and adjusting pH to 4.5 by microliter additions of 3 M HCl. No buffers were used. The BPTI concentration was determined spectrophotometrically (GBC UV-VIS 920) at 280 nm (before addition of dextran), using an extinction coefficient of $0.837 \text{ mL mg}^{-1} \text{ cm}^{-1}$ (Gottschalk et al., 2003a). Volume fractions were calculated with partial specific volumes of 0.611 mL g^{-1} for dextran (Granath, 1958), 0.720 mL g^{-1} for BPTI (Filfil et al., 2004), and 1.000 mL g^{-1} for water. The mixed BPTI/dextran samples were prepared by adding known amounts of

dextran powder to a BPTI solution of known concentration. The relevant concentration variables for all samples are summarized in Table 1: mass (w) and volume (ϕ) fractions, molarities (C), and the number of water molecules per glucose unit (N_W^{glu}) or per BPTI molecule (N_W^{BPTI}). To assess the degree of polymer chain overlap, we include in Table 1 the mean spacing, d , between dextran molecules. For a uniformly expanded face-centered cubic spatial distribution, $d = (\sqrt{2}V_M/\phi_M)^{1/3}$ with ϕ_M the dextran volume fraction and $V_M = 10,540 \text{ \AA}^3$ the anhydrous volume of a dextran molecule.

Relaxation dispersion measurements

The longitudinal relaxation rate of the water ^1H resonance was measured over more than four frequency decades, from 10 kHz to 200 MHz. To cover this frequency range, we used three types of NMR spectrometer: 1), a Stelar Spinmaster (Stelar, Mede, Italy) fast field-cycling (FC) spectrometer (from 10 kHz to 10 MHz); 2), a field-variable iron-core magnet (Drusch, Hanstedt, Germany or GMW, San Carlos, CA) equipped with a Tecmag (Houston, TX) Discovery or Apollo console (16–78 MHz); and 3), Bruker (Billerica, MA) Avance DMX 100 and 200 spectrometers with conventional cryomagnets (100 and 200 MHz). The temperature was maintained at $27.0 \pm 0.1^\circ\text{C}$ using a Stelar variable temperature control unit (below 100 MHz) or a Bruker Eurotherm regulator (at 100 and 200 MHz). Temperatures were checked with a thermocouple referenced to an ice-water bath. No attempt was made to purge oxygen from the solutions, because the small paramagnetic relaxation contribution from dissolved O_2 (Teng et al., 2001) is expected to cancel out when taking the difference of the relaxation rates measured with and without dextran.

In the non-FC experiments (with variable detection field), the longitudinal relaxation rate, R_1 , was measured with the $180^\circ - \tau - 90^\circ$ inversion recovery sequence, an eight-step phase cycle, and 20 randomly ordered delay times. The total ^1H magnetization recovers biexponentially, because it includes not only water and rapidly exchanging macromolecular protons but also a minor contribution from nonexchanging macromolecular protons. The latter contribution, which can increase the apparent R_1 , was eliminated by integrating the water peak over a range where the spectral overlap was negligible (for non-FC experiments), or by using an acquisition delay sufficiently long that the protein magnetization had decayed before the signal was recorded (FC experiments). In this way, single-exponential recovery curves were obtained, from which R_1 was determined by a three-parameter fit. The accuracy of R_1 is estimated to $\pm 1\%$ (one standard deviation).

The FC technique overcomes the sensitivity problem of conventional fixed-field experiments in weak magnetic fields (Noack, 1986; Kimmich and Anardo, 2004). The polarization and detection fields (in ^1H frequency units) were set, respectively, to 20 and 9 MHz (D series of samples) or to 10 and 8 MHz (P series). A field slew rate of 15 MHz ms^{-1} (D series) or 4 MHz ms^{-1} (P series) and a switching time of 3 ms (D series) or 10 ms (P series) were used. Relaxation measurements were performed with two different field

TABLE 1 Concentrations of dextran and BPTI in MRD samples

Sample	w_M^*	ϕ_M^\dagger	$\phi_{\text{BPTI}}^\dagger$	C_{BPTI} (mM)	d (Å)	N_W^{glu}	N_W^{BPTI}
D1	0.090	0.057	—	—	64	91.5	—
D2	0.164	0.107	—	—	52	46.0	—
D3	0.226	0.151	—	—	46	30.8	—
D4	0.279	0.191	—	—	43	23.2	—
D5	0.325	0.227	—	—	40	18.7	—
P0	0	0	0.072	15.4	—	—	3345
P1	—	0.053	0.068	14.5	—	91.5	3417
P2	—	0.100	0.064	13.7	—	46.0	3490
P3	—	0.142	0.061	13.0	—	30.8	3562
P4	—	0.180	0.058	12.4	—	23.2	3634
P5	—	0.214	0.055	11.8	—	18.7	3707

*Mass fraction dextran.

†Volume fraction dextran (M) or BPTI.

cycles (Kimmich and Anardo, 2004): the prepolarized cycle below 10 MHz (D series) or 4 MHz (P series) and the nonpolarized cycle above 4 MHz (P series). In either case, 20 (D series) or 15 (P series) different relaxation delays (evolution times) were used. The magnitude of the quadrature-detected signal after a 90° pulse was recorded with a four-step phase cycle. For the P series, the signal was averaged over 32 transients. The relaxation curves were invariably single exponential. The accuracy (mean \pm SD of 1) of R_1 determined by the FC technique is estimated to 1% (D series) or 1–2% (P series).

Analysis of relaxation dispersion data

The measured ^1H relaxation rate is due to thermal fluctuations of intramolecular and intermolecular magnetic dipole-dipole couplings experienced by water protons and labile macromolecular protons in fast or intermediate exchange (residence time < 10 ms, typically) with the water protons (Venu et al., 1997; Halle et al., 1999). The relaxation dispersion, i.e., the frequency dependence of R_1 , is produced by protons in long-lived (residence time $10^{-9} - 10^{-2}$ s) association with a macromolecule. Such protons belong either to water molecules trapped within the macromolecule or to solvent-exposed hydroxyl, carboxyl, ammonium, or other groups in the macromolecule that engage in rapid proton exchange with water.

Under fast-exchange conditions, the relaxation rate measured on a dextran solution can be expressed as a population-weighted average:

$$R_1(\text{dextran}) = (1 - f_S^M - f_I^M)R_1^{\text{bulk}} + f_S^M R_{1,S}^M + f_I^M R_{1,I}^M + R_1^{O_2}, \quad (1)$$

where $f_I^M = 3/(3 + 2N_W^{\text{glu}})$ is the fraction of the observed protons that reside in dextran hydroxyl groups (three per glucose unit) and $f_S^M = 2N_S^{\text{glu}}/(3 + 2N_W^{\text{glu}})$ is the fraction of the observed protons that reside in water molecules in contact with (and thus significantly dynamically perturbed by) dextran. (The number, N_S^{glu} , of such water molecules is ~ 6 per glucose unit (Uedaira et al., 1989).) Further, R_1^{bulk} is the relaxation rate of oxygen-free bulk water (0.27 s^{-1} at 27 °C; Hindman et al., 1973), $R_1^{O_2}$ is the paramagnetic relaxation enhancement from dissolved oxygen (0.1 s^{-1} for water in equilibrium with air; Teng et al., 2001), and $R_{1,S}^M$ and $R_{1,I}^M$ are, respectively, the intrinsic relaxation rates of protons in water molecules hydrating dextran and in the hydroxyl groups of dextran.

For a solution containing dextran as well as BPTI, the relaxation rate contains additional contributions from internal water molecules (four per BPTI molecule; Venu et al., 1997) and labile BPTI protons (at pH 4.5, mainly the eight hydroxyl groups), with proton fraction f_I^{BPTI} , and from water molecules in the hydration layer of BPTI, with proton fraction f_S^{BPTI} . Thus,

$$R_1(\text{BPTI} + \text{dextran}) = (1 - f_S^M - f_I^M - f_S^{\text{BPTI}} - f_I^{\text{BPTI}})R_1^{\text{bulk}} + f_S^M R_{1,S}^M + f_I^M R_{1,I}^M + f_S^{\text{BPTI}} R_{1,S}^{\text{BPTI}} + f_I^{\text{BPTI}} R_{1,I}^{\text{BPTI}} + R_1^{O_2}. \quad (2)$$

At sufficiently low dextran concentrations, we can assume that the dextran contribution is unaffected by the protein. Also the small oxygen contribution should be the same as without protein. These contributions then cancel out in the difference of the relaxation rates measured on the (BPTI + dextran) sample, henceforth denoted Pn , and on the dextran sample, henceforth denoted Dn , with the same water/glucose mol ratio (see Table 1). Thus,

$$\Delta R_1 \equiv R_1(\text{BPTI} + \text{dextran}) - R_1(\text{dextran}) = (1 - f_S^{\text{BPTI}} - f_I^{\text{BPTI}})R_1^{\text{bulk}} + f_S^{\text{BPTI}} R_{1,S}^{\text{BPTI}} + f_I^{\text{BPTI}} R_{1,I}^{\text{BPTI}}. \quad (3)$$

The frequency dependence of the difference relaxation rate, ΔR_1 , is produced by the last term in Eq. 3. If the residence times of all protons contributing to this term are long compared to the rotational correlation time, τ_R , of the protein, as is the case for BPTI (Denisov et al., 1995, 1996; Venu

et al., 1997; Denisov and Halle, 2002), then the difference dispersion profile, $\Delta R_1(\omega_0)$, from a solution containing BPTI monomers (A) and decamers (B) is described by the following relations (Venu et al., 1997; Halle et al., 1999):

$$\Delta R_1(\omega_0) = \alpha + b_A L_A(\omega_0) + b_B L_B(\omega_0) \quad (4)$$

$$L_X(\omega_0) = (1 - \xi_X) L_X^{\text{intra}}(\omega_0) + \xi_X L_X^{\text{inter}}(\omega_0) \quad (5)$$

$$L_X^{\text{intra}}(\omega_0) = \frac{0.2 \tau_{R,X}}{1 + (\omega_0 \tau_{R,X})^2} + \frac{0.8 \tau_{R,X}}{1 + (2 \omega_0 \tau_{R,X})^2} \quad (6)$$

$$L_X^{\text{inter}}(\omega_0) = \frac{0.3 \tau_{R,X}}{1 + (\omega_0 \tau_{R,X})^2} + \frac{0.6 \tau_{R,X}}{1 + (2 \omega_0 \tau_{R,X})^2}. \quad (7)$$

Here, \square_X is the mean-square fluctuation amplitude and $\tau_{R,X}$ is the rank-two rotational correlation time associated with BPTI oligomer X ($X = A$ for monomer and $X = B$ for decamer). Furthermore, $\xi_X = b_{X,\text{inter}} / b_X$ is the relative contribution from intermolecular dipole-dipole couplings to the overall fluctuation amplitude, $b_X = b_{X,\text{intra}} + b_{X,\text{inter}}$. The functions $L_X(\omega_0)$ will be referred to as Lorentzians, even though they are, in fact, linear combinations of two Lorentzian (reduced) spectral density functions differing by a factor 2 in frequency. Apart from an overall scaling by a factor 0.9, the functions $L_X^{\text{intra}}(\omega_0)$ and $L_X^{\text{inter}}(\omega_0)$ differ very little (Venu et al., 1997). The value of ξ_X therefore has no significant effect on the oligomer fractions that we deduce from the data. We set $\xi_X = 0.33$, as previously found for the four internal water molecules in BPTI (Venu et al., 1997). The quantity α in Eq. 4 represents all frequency-independent contributions to ΔR_1 , including the secular (zero-frequency) intermolecular contribution (Venu et al., 1997).

The experimental difference dispersion data were subjected to nonlinear Marquardt-Levenberg χ^2 minimization (Press et al., 1992) with the model function given by Eqs. 4–7 and with the products $b_X \tau_{R,X}$ constrained to be nonnegative. At the two highest dextran concentrations (samples P4 and P5), it was necessary to include a third (larger) oligomeric species, as found previously at high salt concentrations (Gottschalk et al., 2003a). All five difference dispersions (samples P1–P5) plus the dispersion from the dextran-free BPTI solution (sample P0) were fitted jointly with the correlation times $\tau_{R,A}$ and $\tau_{R,B}$ constrained to have the same values for all samples. The amplitude parameters b_X obtained from the fit can be expressed as (Gottschalk et al., 2003a):

$$b_X = p_X \beta_X, \quad (8)$$

where p_X is the fraction of BPTI molecules that belongs to oligomer species X or, equivalently, the weight fraction of that species. The intrinsic mean-square fluctuation amplitude β_X is proportional to the number of protons (per BPTI monomer) with residence times long enough ($> \tau_{R,X}$) to sample the rotational diffusion of the oligomer but short enough ($< (\beta_X \tau_{R,X})^{-1}$) to act as a relaxation sink for the observed water ^1H magnetization (Halle et al., 1999). A previous MRD study of salt-induced BPTI decamer formation established that, to a good approximation, $\beta_A = \beta_B$ (Gottschalk et al., 2003a). This is, indeed, expected because: 1), the four internal water molecules in the BPTI monomer are conserved in the decamer; 2), the two small, predominantly nonpolar, cavities formed at the intermolecular contacts in the decamer appear to be empty; 3), the central channel in the decamer is too wide to provide the geometric constraints necessary for long-lived hydration; and 4), most of the hydroxyl and carboxyl protons that contribute to the dispersion at pH 4.5 are fully exposed in the decamer (Włodawer et al., 1987; Lubkowski and Włodawer, 1999; Hamiaux et al., 1999, 2000; Gottschalk et al., 2003a). The oligomer fractions, which must sum to unity, can then be obtained as

$$p_X = \frac{b_X}{\sum_X b_X}. \quad (9)$$

Quoted uncertainties in the fitted parameter values correspond to one standard deviation and were obtained by the Monte Carlo method (Press et al., 1992) using 1000 synthetic data sets.

Modeling of the excluded-volume effect

The model used to describe the effect of dextran on the BPTI monomer-decamer equilibrium is outlined in the following Theory section. Here we provide further details about calculations, fits, and choice of geometric parameters.

The decamer fraction, p_B , was calculated self-consistently with the aid of Eqs. 11, 18, and 20–22. For given values of the experimental variables, ϕ_{BPTI} (or C_{BPTI}) and ϕ_M , and of the parameters, K_0 , R_A , R_B , R_M , L_M , and λ_M , we use the following iterative scheme:

1. Set $\ln \Gamma = 0$ initially (ideal solution).
2. Substitute K_0 , C_{BPTI} , and Γ into Eq. 11 and solve for p_B .
3. Calculate Δb_{BPTI} and Δb_M from Eqs. 18, 21, and 22, using p_B and geometric parameters.
4. Calculate $\ln \Gamma$ from Eq. 20.
5. Repeat from step 2 until $\ln \Gamma$ and p_B converge to desired accuracy.

In the analysis of the experimentally determined decamer fraction, p_B , at different dextran volume fractions, ϕ_M , we implement this self-consistent scheme in a nonlinear least-squares fit, with K_0 and λ_M as adjustable parameters. In the calculation of p_B , we take into account the slight variation of the BPTI volume fraction ϕ_{BPTI} (and concentration C_{BPTI}) resulting from dilution by added dextran (see Table 1).

The values of the geometric parameters needed to calculate the crowding effect on p_B were assigned as follows. The radii R_X ($X = A, B$, or M) were obtained by adding a distance $\delta/2$ to the bare radius, R_X^0 , deduced from the macromolecular volume:

$$R_X = R_X^0 + \frac{\delta}{2}. \quad (10)$$

The parameter- δ models solvent-mediated short-range repulsion between the macromolecules. We use a default value of $\delta = 3.0 \text{ \AA}$, corresponding to one water layer. This appears to be consistent with thermodynamic data on the preferential solvation of proteins in glucose/water mixtures (Shimizu and Smith, 2004) and with the linearity of the water ^{17}O magnetic relaxation rate up to very high glucose concentrations (at least 20% by volume) (Uedaira et al., 1989).

The radius of a sphere with the same volume as the BPTI monomer, with molar mass 6.50 kg mol^{-1} and partial specific volume 0.720 mL g^{-1} (Filfil et al., 2004), is $R_A^0 = 12.3 \text{ \AA}$. The BPTI decamer is compact, with a high degree of shape complementarity at the monomer interfaces (Lubkowski and Wlodawer, 1999; Hamiaux et al., 1999, 2000). However, it is pierced by a $10\text{--}15 \text{ \AA}$ wide central channel, with a volume comparable to that of a BPTI monomer. We therefore set $V_B = 12 V_A$, corresponding to $R_B^0 = 12^{1/3} 12.3 = 28.1 \text{ \AA}$. The α -(16)-D-linked glucose monomer of dextran is modeled as a cylinder of length $l_M = 4.4 \text{ \AA}$ (Marszalek et al., 1998). The volume, $\pi R_M^2 l_M$, is obtained from the molar mass of the glucose residue, 162.1 g mol^{-1} , and the partial specific volume of dextran, 0.611 mL g^{-1} (Granath, 1958), yielding $R_M^0 = 3.5 \text{ \AA}$. The contour length of the dextran molecule is $L_M = l_M \bar{\mu} = 282 \text{ \AA}$, with $\bar{\mu} = 64.1$ the average degree of polymerization (see above). Finally, the Kuhn length λ_M is regarded as an adjustable parameter. As expected for the flexible α -(16)-D-glycosidic linkage in dextran, we find that λ_M is an order of magnitude shorter than L_M , as assumed in the derivation of Eq. 17.

THEORY

Analytical treatments of solution nonideality resulting from excluded volume can be based either on the virial expansion (McMillan and Mayer, 1945; Zimm, 1946; Kihara, 1953) or on scaled particle theory (Reiss et al., 1959; Boublík, 1974), whereas numerical treatments make use of simulation techniques or density functional theory (Kinjo and Takada, 2002). Here, we adopt the virial expansion approach, which

(before truncation) is formally exact and which, furthermore, allows the effect of polymer flexibility to be included in a simple way.

The stoichiometric association constant for the monomer-decamer equilibrium, $10 A B$, can be expressed as

$$K = \frac{p_B}{(1 - p_B)^{10}} \frac{1}{10 C_{\text{BPTI}}^9} = K_0 \Gamma, \quad (11)$$

where C_{BPTI} is the total BPTI concentration (see Table 1) and K_0 is the dimensionless “ideal” association constant. The excluded-volume effect on the monomer-decamer equilibrium is described by the crowding factor Γ , which is related to the monomer and decamer activity coefficients through (Minton, 1998)

$$\ln \Gamma = 10 \ln \gamma_A - \ln \gamma_B. \quad (12)$$

According to McMillan-Mayer solution theory, the activity coefficients may be expressed in terms of a virial expansion of the form (Hill, 1986)

$$\ln \gamma_X = \sum_Y B_{XY}^{(2)} n_Y + \sum_Y \sum_Z B_{XYZ}^{(3)} n_Y n_Z + \dots \quad (13)$$

In our case, the summation indices run over three species: BPTI monomer (A) and decamer (B) and dextran (M). We assume that the number densities n_A , n_B , and n_M are sufficiently low that we can truncate the expansion after the first term, involving the second virial coefficient B_{XY} (we henceforth omit the superscript). Furthermore, we assume that the interactions among the three species are short ranged and can be approximated by hard repulsions. The second virial coefficient, B_{XY} , is then simply the covolume, V_{XY} , i.e., the volume excluded by molecule X to the center of molecule Y (or vice versa), averaged over all relative orientations of the two molecules. We thus obtain from Eqs. 12 and 13:

$$\ln \Gamma = \left[(1 - p_B) \Delta V_A + \frac{p_B}{10} \Delta V_B \right] n_{\text{BPTI}} + \Delta V_M n_M, \quad (14)$$

where

$$\Delta V_X = 10 V_{AX} - V_{BX}. \quad (15)$$

To calculate the covolumes V_{XY} , we model the BPTI monomer and decamer as spheres of radii R_A and R_B and the dextran polymer as a flexible cylinder of radius R_M , contour length L_M , and statistical segment length (or Kuhn length) λ_M . The sphere-sphere covolumes V_{AA} , V_{AB} , and V_{BB} are simply

$$V_{XY} = \frac{4\pi}{3} (R_X + R_Y)^3, \quad (16)$$

whereas the sphere-polymer covolumes V_{AM} and V_{BM} are given by (Lue, 1998)

$$V_{XM} = \frac{4\pi}{3}(R_X + R_M)^3 + \pi(R_X + R_M)^2 L_M \Psi_{XM}, \quad (17)$$

where $X = A$ or B and

$$\Psi_{XM} = \frac{1}{(1 + \zeta_{XM})} \times \left[1 + \frac{\alpha \zeta_{XM}(2 + \zeta_{XM})}{2\alpha - 1 + (\alpha - 1)\zeta_{XM} + (1 + \zeta_{XM})(L_M/\lambda_M)^{1/2}} \right], \quad (18)$$

with $\alpha = [32/(3\pi)]^{1/2}$ and

$$\zeta_{XM} = \frac{3}{2} \frac{(R_X + R_M)}{\lambda_M}. \quad (19)$$

Equation 17 is a rational fraction approximation that interpolates between the more well-known rod limit (Ogston, 1970) $\zeta_{XM} \ll 1$, where $\Psi_{XM} = 1$, and the random-coil limit (Jansons and Phillips, 1990) $\zeta_{XM} \gg 1$, where $\Psi_{XM} = 1/\zeta_{XM} + \alpha(\lambda_M/L_M)^{1/2}$. This approximate formula compares favorably with Monte Carlo calculations of the covolume (Lue, 1998). Although Eq. 17 is valid for any ratio of the sphere radius, R_X , to the radius of gyration, R_G , of the polymer, it assumes that the polymer is sufficiently long that $L_M \gg \lambda_M$ (as is the case for our dextran). The original derivation of Eq. 17 (Lue, 1998) and its random-coil limit (Jansons and Phillips, 1990) pertain to a polymer of vanishing thickness ($R_M = 0$). In Eqs. 17–19, we have incorporated the finite thickness of the polymer chain simply by replacing R_X with the distance of closest approach, $R_X + R_M$ (Ogston, 1958).

Combination of Eqs. 14–17 now yields

$$\ln \Gamma = \Delta b_{BPTI} \phi_{BPTI} + \Delta b_M \phi_M, \quad (20)$$

where ϕ_{BPTI} and ϕ_M are the BPTI and dextran volume fractions (see Table 1) and

$$\Delta b_{BPTI} = 80 - \left(1 + \frac{R_B}{R_A}\right)^3 + 2p_B \left[\left(1 + \frac{R_B}{R_A}\right)^3 - 40 - \frac{4}{10} \left(\frac{R_B}{R_A}\right)^3 \right] \quad (21)$$

$$\Delta b_M = 10 \left(1 + \frac{R_A}{R_M}\right)^2 \left[\Psi_{AM} + \frac{4}{3} \frac{(R_A + R_M)}{L_M} \right] - \left(1 + \frac{R_B}{R_M}\right)^2 \left[\Psi_{BM} + \frac{4}{3} \frac{(R_B + R_M)}{L_M} \right]. \quad (22)$$

The first term in Eq. 20 represents the nonideality contribution to the BPTI monomer-decamer equilibrium from the excluded volume of the protein itself. This contribution is often neglected, but it is significant at the relatively high protein concentration used here. Because the protein contribution to $\ln \Gamma$ depends on the decamer fraction p_B , the latter must be calculated self-consistently (see Materials and Methods).

RESULTS AND DISCUSSION

Magnetic relaxation dispersion from dextran solutions

Fig. 1 shows water ^1H MRD profiles recorded from five dextran solutions at pH 4.5, 27.0 °C, and dextran volume fractions ϕ_M in the range 0.057–0.227 (samples D1–D5 in Table 1). Because dextran is highly flexible and unstructured, we do not expect any long-lived water molecules in these samples. Apart from a minor contribution from paramagnetic O_2 (Teng et al., 2001), the observed dispersions can therefore be attributed to the three labile hydroxyl protons per glucose residue in dextran. On the basis of previously reported ^1H CPMG T_2 dispersions from dextran (Hills et al., 1991) and glucose (Hills, 1991) solutions, we estimate that the mean hydroxyl proton residence time is $\tau_H \approx 0.5$ ms under our conditions. Because τ_H is two orders of magnitude shorter than the zero-frequency intrinsic ^1H relaxation time of the hydroxyl protons, estimated as $[R_{1,1}^M(0)] \approx 60$ ms from Eq. 1 and the data in Fig. 1, we are in the fast-exchange regime, as assumed in Eq. 1. This conclusion is corroborated by complete ^1H MRD profiles of sample D2 recorded at pH 3.0 and 6.0 (data not shown).

The spectral density function for the hydroxyl protons in dextran is expected to have a complicated form (Tylianakis et al., 1999; Dejean de la Batie et al., 1988), including contributions from various dipole-dipole couplings (glucose CH protons at 2–3 Å as well as H-bonded water molecules) and various motions (bond librations on 10-ps timescale, localized and cooperative conformational motions in the dextran chain on 1–10-ns timescale, and local-global reorientation modes on timescale 10–100 ns). Furthermore,

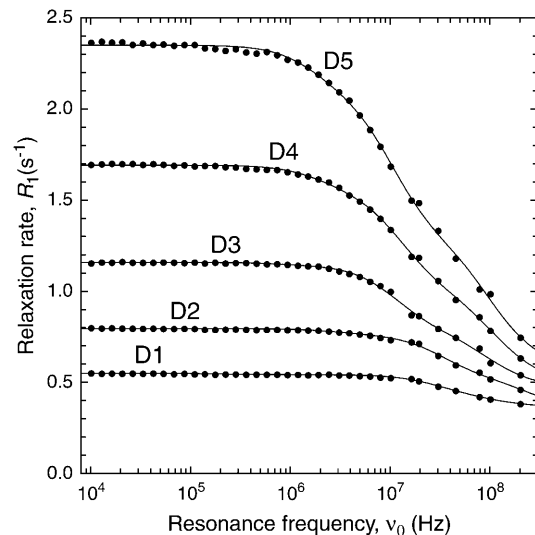


FIGURE 1 ^1H relaxation dispersion profiles from aqueous solutions of dextran at pH 4.5 and 27°C. The dextran concentrations for samples D1–D5 are given in Table 1. The curves were obtained by three-Lorentzian fits as described in the text.

because the high-frequency plateau in the MRD profile is not well defined (see Fig. 1) and because the zero-frequency contribution from the intermolecular (OH-CH) part of $R_{1,I}^M$ is unknown, it is not possible to determine $R_{1,S}^M$ (see Eq. 1) and thereby extract information about dextran hydration dynamics. However, our aim here is not to characterize polymer or water dynamics in dextran solutions. We merely wish to subtract the dextran contribution from the MRD profiles measured on mixed BPTI/dextran solutions. For this purpose, each of the dextran dispersions in Fig. 1 was represented by a three-Lorentzian spectral density function, as in Eqs. 4–6 with $\xi_X = 0$ and one additional Lorentzian. With the aid of the six parameters obtained from each fit (three correlation times τ_k , three associated amplitudes b_k , and a frequency-independent contribution α), the dextran contribution to R_1 can be obtained at any frequency in the range from 10 kHz to 200 MHz.

If the dextran solutions are sufficiently dilute, the correlation times τ_k should be independent of dextran concentration, whereas the amplitude parameters β_k should be proportional to the fraction f_I^M of the observed protons that reside in dextran hydroxyl groups. If the small O_2 contribution is neglected, it then follows from Eq. 1 (because f_S^M is proportional to f_I^M) that the excess relaxation rate $R_1(0) - R_1^{\text{bulk}}$ should be proportional to f_I^M . As seen from Fig. 2, this is the case for samples D1 and D2, whereas the two most concentrated dextran solutions, D4 and D5, show substantial deviations from linearity.

In dilute aqueous solution, dextran behaves as an unstructured, flexible random coil (Nordmeier, 1993; Ioan et al., 2000). The size of the coil may be characterized by the (root-mean square) radius of gyration, R_G . The mean center-to-center separation of adjacent dextran molecules, denoted by d , is given for our samples in Table 1. The dextran solution is

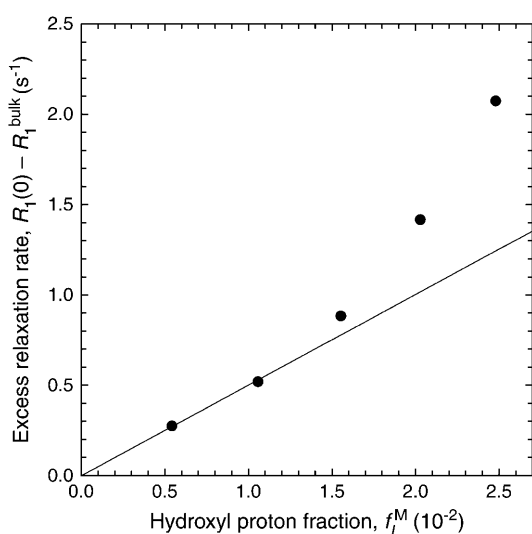


FIGURE 2 Dependence of the zero-frequency excess ^1H relaxation rate, $R_1(0) - R_1^{\text{bulk}}$, in dextran solutions D1–D5 on the dextran hydroxyl proton fraction, f_I^M . The bulk water relaxation rate at 27°C is $R_1^{\text{bulk}} = 0.272 \text{ s}^{-1}$.

said to be dilute if $d > 2R_G$, so that adjacent polymer coils do not interpenetrate extensively. If d is smaller, the coils overlap and the solution is said to be semidilute. The crossover from dilute to semidilute occurs at the overlap concentration, ϕ^* , where the polymers, regarded as spheres of radius R_G , are close packed (on a face-centered cubic lattice). Thus,

$$\phi_M^* = \frac{3V_M}{4\pi R_G^3} \frac{\pi}{3\sqrt{2}}, \quad (23)$$

where the first factor is the dextran volume fraction within a sphere of radius R_G and the second factor is the volume fraction of such spheres at close packing. The radius of gyration has been determined by static light scattering for dextran preparations of higher mean molecular mass than used here, e.g., $R_G = 86 \text{ Å}$ for $\bar{M} = 80 \text{ kg mol}^{-1}$ (corresponding to a contour length, $L_M = 2170 \text{ Å}$) (Nordmeier, 1993) and $R_G = 120 \text{ Å}$ for $\bar{M} = 132 \text{ kg mol}^{-1}$ ($L_M = 3580 \text{ Å}$) (Ioan et al., 2000). For the freely jointed chain model (Flory, 1969),

$$R_G = \left(\frac{\lambda_M L_M}{6} \right)^{1/2}, \quad (24)$$

where λ_M is the Kuhn length. The radii of gyration measured by light scattering thus correspond to $\lambda_M = 20$ and 24 Å . Shorter values of the Kuhn length for dextran have been deduced from hydrodynamic data, $\lambda_M = 13 \text{ Å}$ (Pavlov et al., 1999; and references cited therein), and from single molecule force measurements, $\lambda_M = 8 \text{ Å}$ (Rief et al., 1998) and $\lambda_M = 4.4 \text{ Å}$ (Marszalek et al., 1998). The smallest of these values, equal to the residue length b_M (see above), seems unphysically short; there are surely some steric constraints between adjacent glucose residues. For the following estimates of R_G , we use the value $\lambda_M = 15 \text{ Å}$.

For the $\bar{M} = 10.4 \text{ kg mol}^{-1}$ ($L_M = 282 \text{ Å}$) dextran preparation used for our MRD experiments, Eq. 24 with $\lambda_M = 15 \text{ Å}$ yields $R_G = 26.5 \text{ Å}$. Inserted into Eq. 23, this yields $\phi_M^* = 0.10$. Comparing with the ϕ_M and d values in Table 1, we conclude that samples D1 and D2 are dilute, whereas samples D3–D5 are semidilute. This conclusion is consistent with the experimental findings reported in Fig. 2, where deviations from linearity, signaling overlap of dextran coils, are evident for samples D3–D5. Our analysis is also consistent with previously reported (Tylianakis et al., 1999) ^{13}C relaxation data from solutions of 35 kg mol^{-1} dextran ($R_G = 49 \text{ Å}$ according to Eq. 24 with $\lambda_M = 15 \text{ Å}$), which showed no concentration dependence up to 10% (w/v) dextran (corresponding to $d = 94 \text{ Å}$).

Magnetic relaxation dispersion from BPTI/dextran solutions

^1H MRD profiles were recorded from six BPTI solutions at pH 4.5 with varying amounts of dextran added. The dextran

volume fractions ϕ_M was in the range 0–0.214 (samples P0–P5 in Table 1). In the dextran-free protein solution, only a small fraction of the BPTI molecules are expected to form decamers (Gottschalk et al., 2003a). On addition of dextran, the magnitude of the dispersion step increases markedly. The origin of this increase is twofold. First, there is a direct contribution to the dispersion from the rapidly exchanging hydroxyl protons of dextran (see Fig. 1). Second, there is an indirect effect of macromolecular crowding, whereby the configurational entropy of the dextran molecules shifts the BPTI self-association equilibrium toward the decamer, which produces a much larger dispersion than 10 monomers. To isolate the crowding effect, we subtract the relaxation rate from the corresponding protein-free dextran sample, forming the difference $\Delta R_1 = R_1(\text{BPTI} + \text{dextran}) - R_1(\text{dextran})$. This correction will remove the dextran contribution to $R_1(\text{BPTI} + \text{dextran})$ provided that two conditions are met. First, the water/glucose mol ratio must be the same in the (BPTI+dextran) sample and in the dextran sample. This is the case here (see Table 1). Second, the dextran relaxation contribution must be unaffected by the protein. This is likely to be the case if the dextran concentration is so low that the polymer coils do not overlap (dilute regime) and if the protein does not interact specifically with dextran. As discussed above, we expect these conditions to be met for samples P1 and P2, but not for samples P4 and P5 (sample P3 is a border-line case).

If the direct dextran contribution has been completely removed, the difference dispersion ΔR_1 only reflects labile protons and internal water molecules in BPTI (see Eq. 3). For samples P0–P3, the data are well described by a two-Lorentzian dispersion law as in Eqs. 4–7. For samples P4 and P5, a third Lorentzian component was required. Fig. 3 shows the dispersion from sample P0 and the difference dispersions from samples P1–P5. To exhibit the crowding effect more clearly, we display the normalized rate,

$$\Delta R_1^{\text{norm}} = (\Delta R_1 - \alpha) \frac{N_W^{\text{BPTI}}}{N_{W,\text{norm}}^{\text{BPTI}}}, \quad (25)$$

with $N_{W,\text{norm}}^{\text{BPTI}} = 3500$. This normalization corrects for the variation of the water/BPTI mol ratio, N_W^{BPTI} , with increasing dextran concentration (see Table 1).

The six dispersions in Fig. 3 were fitted jointly with two (samples P0–P3) or three (samples P4 and P5) Lorentzians and with the two shortest correlation times in common for all samples. In all, 24 parameters were thus fitted to 226 data points. These fits are displayed in Fig. 3. The two common correlation times came out as $\tau_1 = 4.3 \pm 0.1$ ns and $\tau_2 = 27.0 \pm 0.5$ ns, close to the values, $\tau_1 = 3.3$ ns and $\tau_2 = 26.3$ ns, expected for the BPTI monomer and decamer in dilute H_2O solution at 27°C and pH 4.5 (Gottschalk et al., 2003a). The slight slowing down of protein tumbling is attributed to dextran (see below), which should have a larger effect on the somewhat elongated monomer (rotational diffusion anisotropy 1.28) than for the nearly spherical decamer (rotational

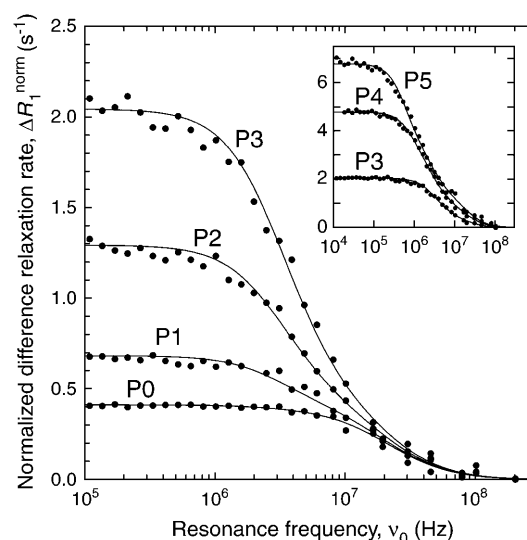


FIGURE 3 ^1H difference relaxation dispersion profiles from aqueous solutions of BPTI and dextran at pH 4.5 and 27°C. BPTI and dextran concentrations for samples P0–P5 are given in Table 1. The curves were obtained by two-Lorentzian (samples P0–P3) or three-Lorentzian (samples P4 and P5) fits as described in the text. The data have been normalized to a water/BPTI mol ratio of $N_W^{\text{BPTI}} = 3500$.

diffusion anisotropy 1.08) (Gottschalk et al., 2003a). The third correlation time obtained from the fit was $\tau_3 = 89 \pm 5$ ns and 147 ± 5 ns for samples P4 and P5, respectively. This is in the same range as observed in previous work (at high salt concentration), where it was attributed to loose clusters of a few decamers (Gottschalk et al., 2003a).

A macromolecular crowding agent, such as dextran, can affect protein rotational diffusion by indirect hydrodynamic interactions as well as by direct potential-derived interactions. Hydrodynamic theory (Cichocki et al., 1999) and Stokesian dynamics simulations (Phillips et al., 1988) yield $\tau_R(\phi) = \tau_R(0)/[1 - 0.6310\phi - 0.726\phi^2 - 0.52\phi^3]$ for a suspension of equal-sized hard spheres at volume fraction ϕ . For $\phi = 0.25$, this becomes $\tau_R(\phi) = 1.27\tau_R(0)$. This modest (27%) retardation is essentially due to configurations where two spheres are very close to contact. In fact, a dominant contribution comes from separations comparable to or less than the size of a water molecule. At such short separations, the validity of the hydrodynamic continuum description may be questioned. If such contact configurations are not present, e.g., because of the energetic cost of removing the first hydration layer from the macromolecules, then the hydrodynamic retardation effect is negligibly small even at high volume fractions (of spherical particles) (Watzlawek and Nägele, 1997). In the presence of soft repulsive forces, the hydrodynamic retardation effect is greatly diminished (Watzlawek and Nägele, 1997). On the other hand, the dextran coils are not compact and therefore permeate space more uniformly than compact spheres. At the higher dextran concentrations, some polysaccharide segments must therefore

be near BPTI molecules and may thus account for the observed (modest) rotational retardation.

Fluorescence anisotropy measurements of protein rotational diffusion in the presence of macromolecular crowding agents have shown stronger retardation effects than expected from hydrodynamic interactions alone, e.g., $\tau_R(\phi)/\tau_R(0) \approx 5$ for green fluorescent protein in the presence of dextran at $\phi = 0.25$ (Swaminathan et al., 1997) and $\tau_R(\phi)/\tau_R(0) \approx 1.4$ (monomer) or 2.5 (flexible dimer) for apomyoglobin in the presence of ribonuclease A at $\phi = 0.18$ (Zorrilla et al., 2004b). These larger retardation factors may be attributed to attractive interactions between the reference protein and the crowding agent. The smaller retardation factor of ~ 1.3 for the BPTI monomer and even less for the BPTI decamer (see above) obtained from our MRD data indicate that the BPTI-dextran interaction is essentially repulsive. In conclusion, whereas a large rotational retardation, as observed in some other systems (Swaminathan et al., 1997; Zorrilla et al., 2004b), is incompatible with these MRD data, a modest retardation has little effect on the data analysis. Fits with the two correlation times τ_1 and τ_2 frozen to their dilute-solution values thus gave essentially the same oligomer populations as obtained when τ_1 and τ_2 were freely adjustable parameters.

The third correlation time was $\tau_3 = 89 \pm 5$ ns and 147 ± 5 ns for samples 4 and 5, respectively. This is in the same range as observed in previous work (at high salt concentration), where it was attributed to loose clusters of a few decamers (Gottschalk et al., 2003a).

The oligomer fractions, p_X , derived from the corresponding dispersion amplitudes, b_X , with the aid of Eq. 9, are given in Table 2. The BPTI decamer fraction is only 1.4% in the absence of dextran, but it increases greatly as dextran is added, reaching 40% for sample P3 at a dextran volume fraction of only 0.14 (see Table 1). For samples P4 and P5, the monomer fraction appears to increase with increasing dextran concentration. We believe that this anomalous behavior is related to the unexpected large increase of the amplitude sum $\sum_X b_X = B$ in going from sample P3 to sample P4 (see Table 2). If the number of long-lived water molecules and labile protons that contribute to the dispersion does not change on self-association of BPTI, then B should be independent of the oligomer fractions. A previous study of salt-induced BPTI decamer formation indicates that this is the case, with $B = (1.1\text{--}1.3)10^8 \text{ s}^{-2}$ (Gottschalk et al., 2003a). The B values of

samples P0–P2 are essentially within this range, whereas sample P3 deviates somewhat and samples P4 and P5 have about threefold larger B values.

Two different scenarios might explain the anomalous behavior of samples P4 and P5. One possibility is that the structure and dynamics of dextran, in the semidilute regime, are significantly perturbed by the protein. In that case, the additivity assumption (see Materials and Methods) would break down so that the direct dextran contribution to $R_1(\text{BPTI} + \text{dextran})$ would not be completely removed by subtracting $R_1(\text{dextran})$ (see Eq. 3). This explanation is consistent with the strong deviations from linearity in Fig. 2 for samples D4 and D5, suggesting a slowing down of chain dynamics on confinement of the polymer coils. Addition of a relatively large amount ($\phi_{\text{BPTI}} \approx 0.06$) of charged protein molecules (along with counterions) to these semidilute dextran solutions might amplify this effect. Another possibility is that dextran affects the structure and dynamics of BPTI in other ways than shifting the monomer-decamer equilibrium. The solubility of BPTI decreases with increasing dextran concentration (Laurent, 1963) and it is therefore conceivable that a fraction of the protein in samples P4 and P5 exists in the form of microaggregates. Either of these two scenarios may be supported by the observation that samples P4 and P5 had a markedly higher viscosity than samples P0–P3 and by the finding that dextran forms a gel at high KCl concentrations (Naji et al., 2003). Further experimental work would be needed to resolve this issue. In the following analysis of the crowding effect, we will only consider the results obtained with samples P0–P3.

Quantitative analysis of macromolecular crowding

We shall now attempt to rationalize the observed dependence of the BPTI decamer fraction, p_B , on the dextran volume fraction, ϕ_M , in terms of statistical-mechanical theory. As described in the Theory section, we use the second-virial approximation and a hard-particle interaction model (only short-range repulsion) to express the nonideality factor $\Gamma = K/K_0$ (see Eq. 11) in terms of the covolumes V_{XY} , with $X = A$ or B and $Y = A, B$, or M . To calculate the covolume, we model the BPTI monomer and decamer as spheres of radius R_A and R_B and the dextran as a freely jointed chain polymer with radius R_M , contour length $L_M = l_M \bar{\mu}$, and Kuhn length λ_M . To model the additional repulsion due to desolvation, we take the distance of closest approach between the centers of two molecular species (A, B , or M) to be the sum of their anhydrous radii R_X^0 (deduced from the known molecular dimensions) and a solvent layer of thickness δ (see Materials and Methods).

Our theoretical analysis differs from most earlier treatments of crowding effects on self-association equilibria in two respects. First, we incorporate the nonideality arising from the excluded volume of the protein itself. Because this effect depends on the oligomer fractions, the calculation must be

TABLE 2 BPTI oligomer fractions derived from MRD data

Sample	100 p_A	100 p_B	100 p_C	$\Sigma b_X (10^8 \text{ s}^{-2})$
P0	98.6 \pm 0.3	1.4 \pm 0.3	–	0.93 \pm 0.02
P1	89.0 \pm 0.5	11.0 \pm 0.5	–	1.05 \pm 0.02
P2	73.2 \pm 0.9	26.8 \pm 0.9	–	1.29 \pm 0.03
P3	60.5 \pm 1.3	39.5 \pm 1.3	–	1.60 \pm 0.05
P4	69.7 \pm 1.5	21.9 \pm 1.4	8.5 \pm 0.8	3.02 \pm 0.09
P5	74.1 \pm 0.9	19.2 \pm 0.8	6.8 \pm 0.3	3.85 \pm 0.09

done self-consistently (see Materials and Methods). For sample P1, where the volume fractions of BPTI and dextran are similar (see Table 1), BPTI and dextran make comparable contributions to the nonideality (see below). The second novel aspect of our analysis is that we model the dextran polymer as a flexible cylinder, rather than as a rigid rod (Ogston, 1970) or a random coil (Jansons and Phillips, 1990). The more general description (Lue, 1998) used here interpolates between these limits. Indeed, the parameter values, $\zeta_{AM} = 1.2$ and $\zeta_{BM} = 2.2$, resulting from our analysis imply that the investigated system is neither in the rod limit ($\zeta_{XM} \ll 1$) nor in the random-coil limit ($\zeta_{XM} \gg 1$).

Fig. 4 shows the result of fitting the model to the experimentally determined decamer fractions for samples P0–P3. The two adjustable parameters obtained from this fit are $\lambda_M = 24 \pm 3$ Å and $K_0 = (1.0 \pm 0.2)10^{12}$. As seen from Fig. 4, the model can account quantitatively for the observed crowding effect and the resulting Kuhn length is similar to the values that have been deduced from light-scattering studies of dextran solutions (Nordmeier, 1993; Ioan et al., 2000). As noted above, single-molecule force measurements (Rief et al., 1998; Marszalek et al., 1998), on the other hand, have suggested a much shorter (in our view, unphysically short) Kuhn length for dextran. The fit in Fig. 4 was performed with $\delta = 3.0$ Å, corresponding to a monolayer of nondisplaceable water for BPTI–BPTI and BPTI–dextran pairs at the distance of closest approach. Equally good fits were obtained with any δ -value in the range 0–4 Å. Fig. 5 shows how the values of the two adjustable parameters, λ_M and K_0 , depend on the fixed δ -value.

Fig. 6 shows how the nonideality factor, Γ , varies with the dextran volume fraction. The quantity $-RT \ln \Gamma$ may be

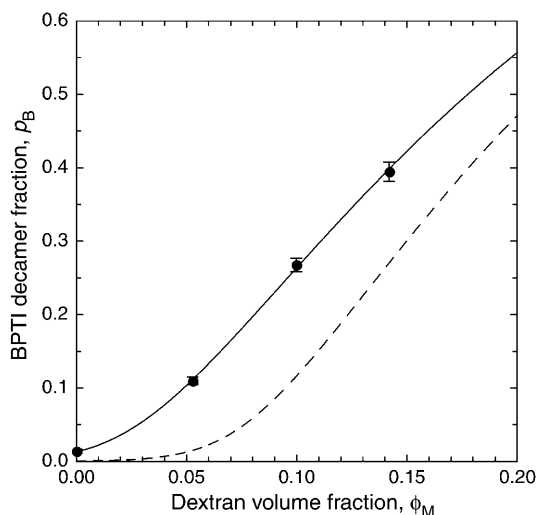


FIGURE 4 The fraction, p_B , of decamer-forming BPTI molecules as a function of dextran volume fraction, ϕ_M . The points were derived from the MRD data (samples P0–P3) and the curve resulted from a fit to the model described in the text (with $\delta = 3.0$ Å). The dashed curve was calculated with the same model parameters, but without the nonideality contribution from BPTI.

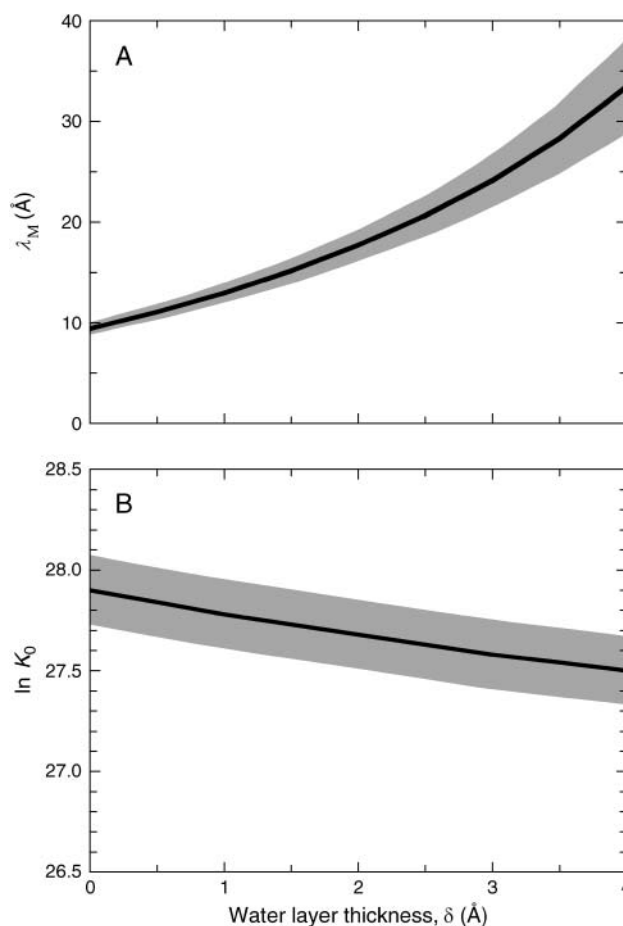


FIGURE 5 Variation of (A) the Kuhn length, λ_M , and (B) the natural logarithm of the ideal association constant, K_0 , with the thickness, δ , of the undisable water layer. The shaded regions correspond to one standard deviation in the fitted parameters.

regarded as the crowding (excluded volume) contribution to the standard free energy of decamer formation for a standard-state BPTI concentration of $C_{BPTI} = 1$ M. We may thus write

$$\Delta G^O = \Delta G_{ideal}^O + \Delta G_{crowd}^O, \quad (26)$$

where $\Delta G_{ideal}^O = -RT \ln K_0 = -16.4 \pm 0.1$ kcal mol⁻¹ (with K_0 obtained from $\delta = 3$ Å fit). The crowding contribution at $\phi_M = 0.14$ (sample P3) is $\Delta G_{crowd}^O = -RT \ln \Gamma = -7.9$ kcal mol⁻¹ (at the standard-state BPTI concentration of $C_{BPTI} = 1$ M), corresponding to a $5.5 \cdot 10^5$ -fold increase of the association constant, K . For this sample, the protein itself contributes -1.4 kcal mol⁻¹ to ΔG_{crowd}^O corresponding to a 10-fold increase of K . In view of Eq. 20, we may write

$$\Delta G_{crowd}^O = -RT(\Delta b_{BPTI} \phi_{BPTI} + \Delta b_M \phi_M). \quad (27)$$

Within the adopted hard-particle model (where partial specific volumes are independent of temperature) and neglecting the weak temperature dependence of Δb_{BPTI} (via p_B) and of Δb_M (via λ_M), this is a purely entropic contribution,

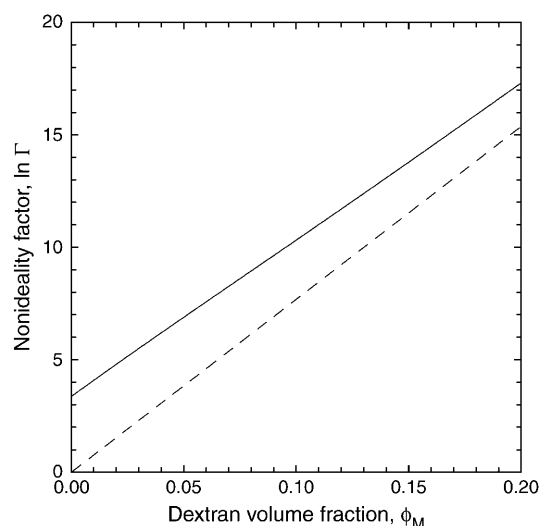


FIGURE 6 Dependence of the natural logarithm of the nonideality factor, Γ , on the dextran volume fraction, ϕ_M . The solid curve was calculated from the model with the parameter values resulting from the fit in Fig. 4. The dashed curve was calculated with the same parameter values, but without the nonideality contribution from BPTI.

i.e., $\Delta G_{\text{crowd}}^{\text{O}} = -T \Delta S_{\text{crowd}}^{\text{O}}$, related to the excess osmotic pressure.

It does not appear to be widely recognized among biochemists and cell biologists that the physical phenomenon underlying the macromolecular crowding effect on protein self-association has received considerable attention by colloid chemists (Kulkarni et al., 2000 and references cited therein). Fifty years ago, Asakura and Oosawa predicted that addition of an inert macromolecular species to a dilute solution of colloidal particles induces an effective attraction between the colloidal particles (Asakura and Oosawa, 1954, 1958). This so-called depletion attraction arises from an imbalance in the local osmotic pressure associated with configurations where the separation between two colloidal particles is too small to accommodate a macromolecule. In an alternative (and equivalent) view, the effective attraction between the colloidal particles is attributed to the increase in accessible volume, and hence configurational (translational) entropy, of the macromolecules as the two colloidal particles approach to contact. The depletion attraction is the origin of the effects described in this work.

CONCLUSIONS

Previous contributions from this laboratory have established field-cycling ^1H MRD as a quantitative method for quantifying coexisting populations of protein oligomers in solution (Gottschalk et al., 2003ab; Gottschalk and Halle, 2003). Here, we have demonstrated that the MRD technique also can be used to study protein self-association in the presence of a second macromolecular species. The ability of

the MRD method to resolve the different oligomeric species on the basis of their rotational correlation times, with little or no influence of long-range (electrostatic or hydrodynamic) interactions is of particular importance in such studies. Provided that the protein and crowding agent contribute independently to the measured relaxation rate, the protein contribution can be isolated by a straight-forward difference experiment. The MRD method can therefore be used also when the crowding agent is another protein. On the other hand, by choosing a crowding agent, such as polyethyleneglycol, without labile protons or trapped water molecules, it is not necessary to perform a difference experiment because the dispersion is then produced exclusively by the self-associating protein.

The results reported here for the effect of dextran on the self-association of BPTI to decameric aggregates have been analyzed with the aid of a statistical-mechanical model that explicitly incorporates polymer flexibility as well as the excluded volume of the protein. This analysis shows that the observed dramatic enhancement of BPTI self-association can be quantitatively rationalized in terms of hard repulsions, with no need to invoke other interactions. Our results thus confirm the prediction that macromolecular crowding at physiologically relevant volume fractions is a potent modulator of self-association equilibria (Minton, 1981, 1998, 2000; Ellis, 2001) with potentially far-reaching biological implications (Garner and Burg, 1994; Walter and Brooks, 1995; Al-Habori, 2001; Hancock, 2004).

We thank Fabian Vaca Chavez, Michael Gottschalk, and Hans Lilja for experimental assistance, and Bayer Healthcare AG (Wuppertal, Germany) for a generous supply of BPTI.

This work was supported by the Swedish Research Council and the Wenner-Gren Foundations.

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